Math 48A, Exam 2
Lessons 4, 5, 6, 7, and 8

## 1. IDENTIFY LINEAR FUNCTIONS USING EQUATIONS

Which of the following equations represent linear functions?
a. $3 y=5 x-2$ $\qquad$ linear function $\qquad$ not a linear function
b. $y=x^{2}-7$
___ linear function $\qquad$ not a linear function
c. $y=\frac{2}{x}-5$ $\qquad$ linear function $\qquad$ not a linear function
d. $y^{2}=4 x-7$ $\qquad$ linear function $\qquad$ not a linear function

Below are tables for two different functions. One of these tables has points from a linear function, and the other does not.

| $x$ | $f(x)$ |
| :---: | :---: |
| -8 | 2 |
| -4 | 4 |
| -1 | 6 |
| 1 | 8 |
| 2 | 10 |


| $x$ | $g(x)$ |
| :---: | :---: |
| -6 | 14 |
| -4 | 10 |
| -1 | 4 |
| 1 | 0 |
| 2 | -2 |

2A. Which function is linear? Explain your reasoning.

2B. Write an equation for the linear function. Justify your answer.
$\qquad$
3. EVALUATE FUNCTIONS USING GRAPHS

Below are graphs of functions $f(x)$ and $g(x)$.


Use the graphs above to evaluate each of the following:

$$
f(-1)
$$

Challenge Problems: Use the graphs to evaluate each of the following:

$$
f(g(0))
$$

$$
\mathrm{g}(f(5))
$$

Consider the following absolute value equation:

$$
|2 x-4|-5=1
$$

Solve this equation using an algebraic method (not graphically). Hint: you might check your work by solving problem 5A below and looking back at this problem.
$\qquad$

## 5. SOLVE ABSOLUTE VALUE EQUATIONS GRAPHICALLY

5A. Consider the following absolute value equation:

$$
|2 x-4|-5=1
$$

Use the left-hand side (LHS) and right-hand side (RHS) of this equation to a table of values and draw the resulting graph on the axes below. Then, solve this equation using the information in your graph.


| $x$ | LHS | RHS |
| ---: | :--- | :--- |
| -6 |  |  |
| -5 |  |  |
| -4 |  |  |
| -3 |  |  |

Name:

| -2 |  |  |
| ---: | ---: | ---: |
| -1 |  |  |
| 0 |  |  |
| 4 |  |  |
| 5 |  |  |
| 1 |  |  |
| 2 |  |  |
| 3 |  |  |
| 4 |  |  |
| 6 |  |  |

5B. Redraw your graph from problem 5A in the axes below. Then consider the absolute value inequality:

$$
|2 x-4|-5 \geq 1
$$

Using your graph, identify all $x$-values that solve this equation.

Name:

$\qquad$

## 6. ANALYZE THE GRAPH OF A FUNCTION

Below is a graph of a function $f(x)$.


Use the graph to answer each of the following questions about the function $f$. For some of your answers you may need to approximate the value. Please give a decimal approximation using your best judgment based on the graph.

6 A. What is $f(-5)$ ?
6B. What is $f(0)$ ?

6 C. Find the $x$ values for which $f(x)=0$.

6D. Find the $x$ values for which $f(x) \leq 3$.
6E. Find the $x$ values for which $f(x)>9$

## 7. ANALYZE THE GRAPH OF A FUNCTION

Below is a graph of a function $k(x)$. Use the graph to answer the questions about the function.


7A. At what point(s) does $k(x)$ have a local maximum?

7B. On what interval(s) is $k(x)$ decreasing.

7C. $\quad$ Find the average rate of change of $k(x)$ from $x=0$ to $x=3$.
8. EVALUATE FUNCTIONS

For all problems below, let $f(x)=x^{2}-x+3$.
8A. Evaluate $f(3)$

8B. Evaluate $f(-5)$

Name:
8C. If $f(x)=x^{2}-x+3$, then evaluate $f(2 a)$

8D. If $f(x)=x^{2}-x+3$, then evaluate $f(a+h)$

The following is a graph of a piecewise defined function $g(x)$. Find the formula (rule) for each part of the function and the $x$-values for which it applies. Explain your reasoning.


$$
g(x)= \begin{cases}\text { if } \\ & \text { if } \\ & \text { if }\end{cases}
$$

