

Name : _____

Math 1C, Lesson 7: In-Class Problems

Class Number: _____

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1. Suppose $z = f(x, y)$ is a two-variable function and let $z_0 \in \mathbb{R}$ be a constant value in the range of the function f .
- What is the definition of the contour curve $C_{z_0}(f)$?
 - What is the definition of the level curve $L_{z_0}(f)$?
 - Describe the similarities and differences between $L_{z_0}(f)$ and $C_{z_0}(f)$?
 - Describe how level curves are related to contour curves?
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2. Find the domain and range of the function $f(x, y) = \sqrt{80 - 5x^2 - 5y^2}$
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3. Graph several level curves of the function $z = x^2 + \frac{y^2}{9}$.
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4. Identify the trace of the surface $\frac{x^2}{6} + 24y^2 + \frac{z^2}{24} - 6 = 0$ in the plane $y = 0$.
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5. Consider the function

$$z = x^2 + y^2 - 16.$$

find a parametric equation to the tangent line of the level curve $L_0(f)$ at the point $(-2\sqrt{2}, -2\sqrt{2})$. Then, graph this level curve and its tangent line.

6. Use a scalar projection to show that the distance from point $P(x_1, y_1)$ to line $ax + by + c = 0$ is

$$\frac{|ax_1 + by_1 + c|}{\sqrt{a^2 + b^2}}.$$

Draw a diagram and explain your reasoning in detail using full sentences.