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LESSON 9: Rational Expressions and Functions

- Polynomial expressions
$\square$ Rational expressions
$\square$ Rational functions
$\square$ Simplified rational expressions
$\square$ Caution on canceling


## ALGEBRAIC PROPERTIES OF FRACTIONS

Rational Number: a number that can be expressed as the quotient of two integers

$$
\frac{550}{5} \leftarrow
$$

Fraction Notation for 1:

$$
\frac{A}{A}=
$$

Multiplication of Fractions: $\quad \frac{A}{B} \cdot \frac{C}{D}=$

Division of Fractions: $\quad \frac{A}{B} \div \frac{C}{D}=$

Addition of Fractions: $\quad \frac{A}{D}+\frac{B}{D}=$

Addition of Fractions: $\quad \frac{A}{D}-\frac{B}{D}=$

## LESSON 9: EQUIVALENT FRACTIONS

Start with the number on the left and use a series of operations to create the equivalent expression on the right. Remember, you can change the way a number looks without changing the VALUE by multiplying or dividing by 1 (in any form you want).

Start with:
End with:
7. $5=$
$=\frac{30 y}{6 y}$
8. $2=$
$=\frac{4 x^{2}}{2 x^{2}}$
9. $1=$
$=\frac{x+5}{5+x}$
10. $-1=$

$$
=\frac{3-x}{x-3}
$$

LESSON 9: EQUIVALENT FUNCTIONS

Fill in the tables below. You can use your graphing calculator or you can do the computations by hand.

1. $\quad f(x)=-2 x$

| $x$ | $f(x)$ |
| :---: | :---: |
| -1 |  |
| 1 |  |
| 3 |  |
| 5 |  |
| 7 |  |

2. $g(x)=\frac{6 x-2 x^{2}}{x-3}$

| $x$ | $g(x)$ |
| :---: | :---: |
| -1 |  |
| 1 |  |
| 3 |  |
| 5 |  |
| 7 |  |

3. Compare the output values of $f(x)$ to $g(x)$. What do you notice?
4. Use the algebraic properties of fractions to validate your observations from problem 3 above.

LESSON 9: Multiplication and Division
$\square$ The product of two rational expressions
$\square$ The quotient of two rational expressions

Using the rules of fractions that we've studied together, multiply or divide the following rational expressions.
5. $\frac{16}{25} \cdot \frac{35}{12}$
6. $\frac{x-1}{x+2} \cdot \frac{x^{2}+2 x}{3-3 x}$

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7. $\frac{10 t+20}{2 t^{2}-3 t+1} \cdot \frac{t^{2}-1}{5 t+10}$
8. $\frac{x^{2}-2 x-3}{x^{2}-4} \div \frac{3-x}{x+2}$

OPTIONAL CHALLENGE PROBLEMS
9. $\frac{\left(a^{2}+3 a+2\right)}{a^{2}-4} \div \frac{5 a^{2}+10 a}{a-2}$
10. $\frac{10 b+20}{b} \cdot \frac{b^{2}}{b+2}$

