

## SECTION 5.5: Multiplication of Polynomials (p. 380 – 387)

- Multiply monomials (p. 381)
- Distributive law:  $a \cdot (b \pm c) = a \cdot b \pm a \cdot c$
- The product of a monomial and a polynomial (p. 382)
- The product of two polynomials (p. 383)

Multiply each of the following. Show all steps.

$$\begin{aligned}
 1. \quad (2x - 1)(x - 8) &= 2x(x - 8) - 1 \cdot (x - 8) \\
 &= 2x^2 - 16x - x + 8 \\
 &= \boxed{2x^2 - 17x + 8}
 \end{aligned}$$

$$\begin{aligned}
 2. \quad (t - 3)^2 &= (t - 3) \cdot (t - 3) \\
 &= t \cdot (t - 3) - 3 \cdot (t - 3) \\
 &= t^2 - 3t - 3t + 9 \\
 &= \boxed{t^2 - 6t + 9}
 \end{aligned}$$

Note on Notation

• Any time we write

$$b^2 = b \cdot b$$

for any base  $b$ , we call this a perfect square.

$$\begin{aligned}
 3. \quad (3y + 2)(y - 5) &= 3y \cdot (y - 5) + 2 \cdot (y - 5) \\
 &= 3y^2 - 15y + 2y - 10 \\
 &= \boxed{3y^2 - 13y - 10}
 \end{aligned}$$

$$\begin{aligned}
 4. \quad (2p-7)^2 &= (2p-7) \cdot (2p-7) \\
 &= 2p \cdot (2p-7) - 7 \cdot (2p-7) \\
 &= 4p^2 - 14p - 14p + 49 \\
 &= \boxed{4p^2 - 28p + 49}
 \end{aligned}$$

Note on Notation  
 • When we write the perfect square of a binomial  $(A+B)^2$  as a trinomial given by  $A^2 + 2AB + B^2$  we call this a perfect-square trinomial (it comes from a perfect square)

### VII. FACTOR BY GROUPING (6.1 p. 439)

Factor completely using the factor by group technique:

$$\begin{aligned}
 5. \quad x^2 - x + 3x - 3 &= (x^2 - x) + (3x - 3) \\
 &= x \cdot (x - 1) + 3 \cdot (x - 1) \\
 &= \boxed{(x + 3) \cdot (x - 1)}
 \end{aligned}$$

$$\begin{aligned}
 6. \quad 2m^2 - 6m + 5m - 15 &= (2m^2 - 6m) + (5m - 15) \\
 &= 2m \cdot (m - 3) + 5 \cdot (m - 3) \\
 &= \boxed{(2m + 5) \cdot (m - 3)}
 \end{aligned}$$

SECTION 6.3: Trinomials of the type  $ax^2 + bx + c$  (p. 455 - 464)

- The FOIL Method to factoring:  $ax^2 + bx + c$  (p. 455 - 456)
- Tips for factoring  $ax^2 + bx + c$  with FOIL (p. 458)
- The AC Method to factoring:  $ax^2 + bx + c$  (p. 458 - 459)
- Algebraic and graphical approach to solving  $ax^2 + bx + c = 0$  (p. 461)

Solve each of the following quadratic equations using the zero product property:

7.  $n^2 + 3n - 54 = 0$

$a=1, b=3, c=-54$

$\Rightarrow n^2 + 9n - 6n - 54 = 0$

$\Rightarrow n(n+9) - 6(n+9) = 0$

$\Rightarrow (n-6) \cdot (n+9) = 0$

$\Rightarrow n-6 = 0$  or  $n+9 = 0$

$\Rightarrow \boxed{n=6}$  or  $\boxed{n=-9}$

Multiply

$$\begin{array}{r} \cancel{-54} \\ 9 \quad \cancel{-6} \\ \quad \quad \cancel{+3} \end{array}$$

Add

$\Rightarrow 3n = 9n - 6n$

8.  $3x^2 + x - 4 = 0$

$a=3, b=1, c=-4$

$\Rightarrow 3x^2 - 3x + 4x - 4 = 0$

$\Rightarrow 3x \cdot (x-1) + 4 \cdot (x-1) = 0$

$\Rightarrow (3x+4) \cdot (x-1) = 0$

$\Rightarrow 3x+4 = 0$  or  $x-1 = 0$

$\Rightarrow \boxed{x = -4/3}$  or  $\boxed{x = 1}$

Multiply

$$\begin{array}{r} \cancel{-12} \\ +4 \quad \cancel{-3} \\ \quad \quad \cancel{+1} \end{array}$$

Add

$1x = 4x - 3x$

$$9. \quad w^2 = -18w \quad \Rightarrow \quad w^2 + 18w = 0$$

$$\Rightarrow \quad w \cdot (w + 18) = 0$$

$$\Rightarrow \quad w = 0 \quad \text{or} \quad w + 18 = 0$$

$$\Rightarrow \quad \boxed{w = 0} \quad \text{or} \quad \boxed{w = -18}$$

$$10. \quad 4w^2 + 20w + 25 = 0$$

$$a=4, \quad b=20, \quad c=25$$

$$\Rightarrow \quad 4w^2 + 10w + 10w + 25 = 0$$

Multiply

$$\begin{array}{ccc} & 100 & \\ 10 & \times & 10 \\ & 20 & \end{array}$$

Add

$$\Rightarrow \quad \underline{20w} = 10w + 10w$$

$$\Rightarrow \quad 2w(2w + 5) + 5 \cdot (2w + 5) = 0$$

$$\Rightarrow \quad (2w + 5) \cdot (2w + 5) = 0$$

$$\Rightarrow \quad \boxed{2w + 5} = 0$$

$$\Rightarrow \quad 2w = -5$$

$$\Rightarrow \quad \boxed{w = -\frac{5}{2} = -2.5}$$